### Survey on Different Leakage Models

### Krzysztof Pietrzak



Centrum Wiskunde & Informatica

### crypto in the clouds, MIT Boston, Aug. 4th 2009

- Proveable security is a big success story.
   Last 30 years: Strong security notions & matching constructions for all important primitives.
- Security notions (mostly from mid 80ies) consider security game where cryptosystem is an idealized black-box.
- This notion do not capture "physical attacks" that became more relevant in the last 1-2 decades.
  - Side-channell attacks are a thread to leight-weight devices (RFIDs, smart-cards).
  - Malware attacks (viruses, Trojans) are a thread for heighly connected (i.e. over the Internet).





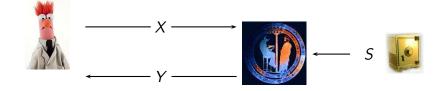
# Side-Channel Attacks

# Malware

Security Fall

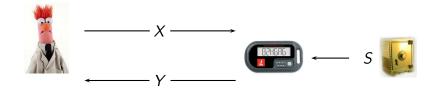
viruses/trojans

Krzysztof Pietrzak Survey on Different Leakage Models

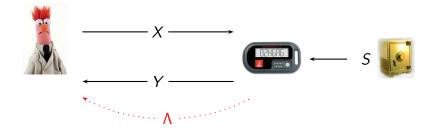


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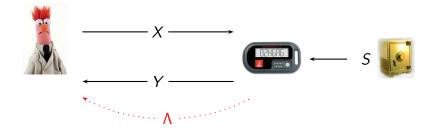
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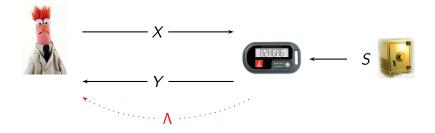
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- In the physical world the adversary can attack an *implementation*.
- Possibly can extract information A.
- To get secure *implementations* we need security notions which take leakage Λ into account.
- Leakage  $\Lambda = f(S, R, X)$  is a function of secret state S, input X and random coins R.

### Part 1: Particular leakage functions.

- Exposure Resilience (against cold-boot attacks).
- Private Circuits (against probing attacks).
- Part 2: General leakage functions.
  - Memory attacks, aka. bounded leakage.
  - Auxiliary Input.
  - Bounded leakage & Auxiliary Input are incompareable.
- Part 3: Unbounded leakage.
  - Bounded-Retrieval Model (against malware).
  - Leakage-Resilience (against side-channel attacks).
  - Extensions/Restrictions of leakage-resilience.

- Anything on active attacks (fault attacks, tamper-resistance).
- Proactive-Security, Forward-Security, Intrusion-Resilience, Crypto without "perfect shredding" [CEGL08], one-time programs [GTKR08],...
- 1000+ papers from a practical perspective (e.g. anything from CHES).

### Part 1: Particular leakage functions

- Exposure Resilience (against cold-boot attacks).
- Private Circuits (against probing attacks).

### cold-boot attacks



... the attack relies on the data remanence property of DRAM and SRAM to retrieve memory contents which remain readable in the seconds to minutes after power has been removed.

J. Alex Halderman, Seth D. Schoen, Nadia Heninger, William Clarkson, William Paul, Joseph A. Calandrino, Ariel J. Feldman, Jacob Appelbaum, and Edward W. Felten Lest We Remember: Cold Boot Attacks on Encryption Keys. In USENIX 2008.

### Exposure-Resilient Cryptography

- B. Chor, O. Goldreich, J. Håstad, J. Friedman, S. Rudich, R. Smolensky
   The Bit Extraction Problem of t-Resilient Functions In *FOCS* 1985.
- R. Canetti, Y. Dodis, S. Halevi, E. Kushilevitz, A. Sahai. Exposure-resilient functions and all-or-nothing transforms In EUROCRYPT 2000.
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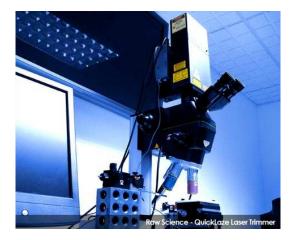
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  - Leakage  $\Lambda = f(M)$  are some bits of memory M.
  - Don't keep secret S in plain on memory but encode using "t-resilient function" g

$$ENC(S) = [R, g(R) \oplus S]$$
 R random

g(.) is *t*-resilient means g(R) is uniform even when given *t* bits of *R*.

## Probing attacks



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### **Private Circuits**

- Y. Ishai, A. Sahai, and D. Wagner. Private Circuits: Securing Hardware against Probing Attacks In CRYPTO 2003.
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  - For any t ∈ N, show how to transform any circuit C(.) into a circuit C<sub>t</sub>(.) such that

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- **2** Value on any t wires of  $C_t(S)$  are independent of S.
- Uses techniques from general multiparty computation. Big blowup,  $|C_t| \approx t^2 |C|$ .

### Part 2: General leakage functions

- Memory attacks, aka. bounded leakage.
- Auxiliary Input.
- Bounded leakage & Auxiliary Input are incompareable.

• Leakage  $\Lambda = f(S)$  where

$$f: \{0,1\}^* 
ightarrow \{0,1\}^\lambda$$

can be any (adversarially chosen) function with bounded range (to  $\lambda \in \mathbb{N}$  bits).

 Can extend any standard security notion (ind-CPA/CCA, unforgeability) by additonally assuming that the adversary gets leakage Λ. Observation (Every sig. scheme is secure againts memory attacks with security loss exponential in  $\lambda$ .)

If signature scheme Sig cannot be forged with advantage  $\epsilon$ , then it cannot be forged with advantage  $\epsilon \cdot 2^{\lambda}$  in a  $\lambda$ -memory attack (by adversaries of the same size).

- Similar results hold for encryption schemes, weak PRFs, but not for PRFs, PRGs.
- Is the exponential loss necessary? Yes in general.
- Next slide: particular constructions of signature/encryption schemes where the security does not degrade with λ (and λ can be as big as a constant fraction of the key-length).

### "security against memory attacks" bibliography

- Adi Akavia, Shafi Goldwasser, Vinod Vaikuntanathan Simultaneous Hardcore Bits and Cryptography against Memory Attacks TCC'09
- M. Naor, G. Segev Public-Key Cryptosystems Resilient to Key Leakage Crypto'09.
- 3 J. Katz, V. Vaikuntanathan

Signature schemes with bounded leakage resilience *Eprint* 2009/220.

Joel Alwen and Yevgeniy Dodis and Daniel Wichs Public Key Cryptography in the Bounded Retrieval Model and Security Against Side-Channel Attacks Crypto'09

### Signature schemes secure against memory attacks

Let Sig be a signature scheme constructed via Fiat-Shamir transform from a witness-indistinguishable  $\Sigma$ -protocol where each *pk* corresponds to exponentially many (say 2<sup>*m*</sup>) different *sk* (e.g. Okamoto).

### Theorem (KV09, ADW09 informal)

If Sig cannot be forged with advantage  $\epsilon$ , then it cannot be forged with advantage  $\epsilon$  even in  $\lambda$ -memory attack where  $\lambda$  is almost m.

Can choose *m* as large as  $(1 - \delta)|sk|$  for any  $\delta > 0$ . Then no expontial degradation in security (in fact, no degradation at all) even if almost all the key is leaked

## Auxilliary Input

Leakage  $\Lambda = f(S)$  where  $f : \{0, 1\}^* \to \{0, 1\}^{\lambda}$  can be any function that is exponentially hard to invert

 $\exists \alpha > 0 \ \forall \text{PPT } A \ \exists n' \ \forall n > n' : \Pr_{x \leftarrow \{0,1\}^n}[A(f(x)) = x] \le 2^{-\alpha \cdot n}$ 

Yevgeniy Dodis, Yael Tauman Kalai and Shachar Lovett On Cryptography with Auxiliary Input STOC'09

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Learing Paritiv with noise:  $\{A, Ax + e\} \stackrel{c}{=} \{A, U\}$  $A \in_R \{0, 1\}^{t \times n}, x \in_R \{0, 1\}^n$  and e is a error vector.

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- Then f is exponentially hard to invert

 $\Pr_{x \in_{R}\{0,1\}^{n}}[A(f(x)) = x] \le 2^{-H_{\infty}(x|f(x))} \le 2^{\lambda - n} = 2^{-n/2}$ 

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- What is actually required is not  $|f(x)| = \lambda$ , but  $H_{\infty}(x|f(x)) \ge n \lambda$
- And in fact only a computational version of this

$$H_{s,\epsilon}^{HILL}(x|f(x)) \geq n - \lambda$$

### Definition (HILL pseudoentropy [HåstadILL99], [BarakSW03])

X has *HILL* pseudoentropy k, denoted  $\mathbf{H}_{\epsilon,s}^{\text{HILL}}(X) \ge k$ , if  $\exists Y$  s.t.  $\mathbf{H}_{\infty}(Y) \ge k$  and no A of size s can distinguish X from Y with advantage  $\epsilon$ .

So what we have to compare are f(.) (and say  $\lambda = n/2$ ) where

$$H_{\infty}(x|f(x)) \geq n - \lambda$$

3 
$$\Pr_{x \in_R \{0,1\}^n}[A(f(x)) = x] \le 2^{-\alpha n}$$
 for some  $\alpha > 0$ 

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$$Pr_{x \in_R \{0,1\}^n}[A(f(x)) = x] \le 2^{-\alpha n} \text{ for some } \alpha > 0$$

• Assume f(.) is an exponentially hard to invert one-way permutation, i.e.

$$\Pr[A(f(x)) = x] \le 2^{-\alpha n}$$

but

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So satisfies aux. input (2) but not bounded leakage (1).

So what we have to compare are f(.) (and say  $\lambda = n/2$ ) where

$$\begin{array}{l} \bullet \quad H_{\infty}(x|f(x)) \geq n - \lambda \\ \bullet \quad \mathsf{Pr}_{x \in_{R}\{0,1\}^{n}}[A(f(x)) = x] \leq 2^{-\alpha n} \text{ for some } \alpha > 0 \end{array}$$

Let  $\phi : \{0,1\}^n \to \{0,1\}^n \cup \bot$   $\Pr[\phi(x) = x] = 2^{-n^{0.5}}$   $\Pr[\phi(x) = \bot] = 1 - 2^{-n^{0.5}}$ •  $\exists A : \Pr[A(\phi(x)) = x] = 2^{-n^{0.5}} \gg 2^{-\alpha n}$ •  $H_{\infty}(x|\phi(x)) = n$  (with prob.  $1 - 2^{-n^{0.5}}$ ). So satisfies bounded leakage (1) but not aux. input (2).

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### Bounded-leakage & Auxilliary input are incompareable

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#### Part 3: Unbounded leakage

- Bounded-Retrieval Model (against malware).
- Leakage-Resilience (against side-channel attacks).
- Bounded-leakage vs. Auxilliary-input against side-channel attacks.

# Bounded-Retrieval Model [D06,CLW06,...]





• Challange: protect against malware that (temporarily) controls your computer on which a secret key *sk* is stored.

# Bounded-Retrieval Model [D06,CLW06,...]





- Challange: protect against malware that (temporarily) controls your computer on which a secret key sk is stored.
- Bounded Retrieval Model: malware has complete control over the computer but can only send out a bounded amout of information (1GB say).

# Bounded-Retrieval Model [D06,CLW06,...]





- Idea, make sk huge (2GB say) and design a scheme that remains secure even when f(sk) is leaked for any f where  $|f(sk)| \le 1GB$ .
- The efficiency of the scheme schould only depend on some security parameter *n* but not on |sk|. So can't simply use schemes secure againts memory attacks with huge keys.



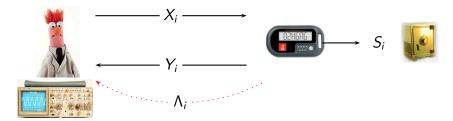
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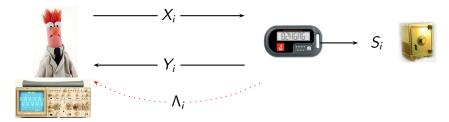


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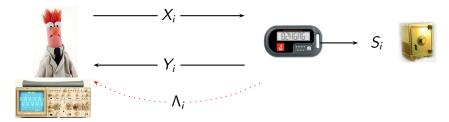
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• Adversary measures leakage  $\Lambda_1, \Lambda_2, \ldots$  on each invocation.

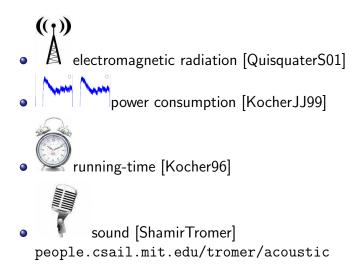


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- Security against λ-memory attacks insufficient as
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- Adversary measures leakage  $\Lambda_1, \Lambda_2, \ldots$  on each invocation.
- Security against  $\lambda$ -memory attacks insufficient as  $|\Lambda_1| + |\Lambda_2| + \ldots$  can be arbitrary large.
- Bounded-retrieval model inconvienient (huge keys) and a priori bound on queries.

# Side-Channels



• Most general leakage model:

 $\Lambda_i = f(X_i, R_i, S_{i-1})$ 

- The *i*th input  $X_i$
- The random coins *R<sub>i</sub>* used during the *i*th invocation.
- The secret internal state  $S_{i-1}$ .

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- This model is clearly too strong, e.g. we can leak the entire internal state  $\Lambda_1 = S_0$ .
- We must add restrictions on f(.) which should be



- sufficient: allow for actual leakage-resilient constructions.
- general: should cover almost all side-channel attacks.

Restricting the leakage function  $\Lambda_i = f(X_i, R_i, S_{i-1})$ 

Sounded leakage:  $|\Lambda_i| = \lambda$  for a leakage parameter  $\lambda \ll |S|$ .

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Restricting the leakage function  $\Lambda_i = f(X_i, R_i, S_{i-1})$ 

- Sounded leakage:  $|\Lambda_i| = \lambda$  for a leakage parameter  $\lambda \ll |S|$ .
- Subscription Efficient: f(.) must be efficient [MR03 Ax5].
- Only computation leaks information [MR03 Ax1]:

$$\Lambda_i = f(X_i, R_i, S_{i-1}^+)$$

where  $S_{i-1}^+ \subseteq S_{i-1}$  is the part of the state that is *accessed* on the *i*th invocation.

## Side-Channel Countermeasures Design Process

#### Currently (exaggerated)

- Implement primitive.
- Find a side-channel attack.
- Sind & implement a fix.
- Goto step 2.

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- Using Leakage-Resilience
  - Consider a general class *F* of leakage-functions (cf. next slide).
  - Cryptography: Design a primitive and *prove* it's secure against side-channels in *F*.
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  - Consider a general class *F* of leakage-functions (cf. next slide).
  - Cryptography: Design a primitive and *prove* it's secure against side-channels in *F*.
- Engineering: Design hardware whose leakage is in *F*.
   Advantage: modular and you can blame someone if it fails.

## Leakage-Resilient Cryptography biblography

#### S.Dziembowski and K.P.

Leakage-Resilient Cryptography (Stream-Cipher in standard model) FOCS'08

#### 2 K.P.

A Leakage-Resilient Mode of Operation EUROCRYPT'09

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How to Secure ElGamal against Side-Channel Attacks (PKE in generic group model) manuscript'09

S.Faust, E.Kiltz, K.P and G.Rothblum Leakage-Resilient Signatures (standard model) eprint 2009/282

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Open problems: LR block-cipher? LR PKE in standard model? generic compiler (à la private circuits)?

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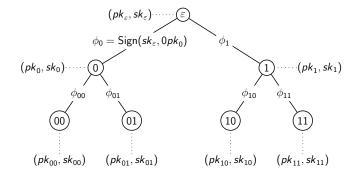
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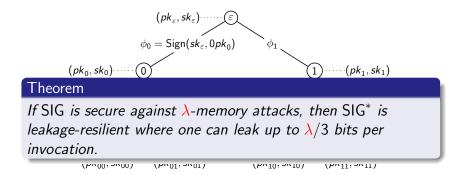
Leakage-resilient primitives are inherently stateful. LR achieved either by key-evolution [1,2,4] or secret-sharing [3].

## Leakage-Resilient Signatures



Tree based signatures: use signature-scheme
 SIG = (KG, Sign, Vfy) that can sign up to 3 messages in a tree mode to get a scheme SIG\*.

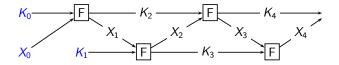
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## A Leakage-Resilient Mode of Operation [P09]

- $F: \{0,1\}^{\kappa} \times \{0,1\}^n \to \{0,1\}^{\kappa+n}$
- Secret key is  $K_0, K_1, X_0$ , output is  $X_1, X_2, \ldots$
- *i*'th round:  $(K_{i+2}, K_{i+1}) \leftarrow F(K_i, X_i)$ .



#### Theorem

This is a leakage resilient stream-cipher if instantiated with any weak PRF F.

• Simpler & more efficient than [Dziembowski-P FOCS'08] where we used PRGs & Extractors.

## Extensions/Restrictions of leakage-resilience

Adversary can choose leakage functions f<sub>1</sub>, f<sub>2</sub>,...
 adaptively. In a weaker non-adaptive model (i.e.
 f<sub>1</sub> = f<sub>2</sub> = ...) much more seems possible [SPYQYO09]

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- Potentially can get rid of the "noly computation leaks information" assumption by
  - Low complexity leakage functions.
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- Next Slide: Leakage-resilince can be seen as a continious version of security against memory attacks. Can also consider a continious version of security against auxilliary input.

In side-channel attacks one often measures *lots* of data from which only few bits  $X, |X| \ll |S|$  are extracted and kept for further analysis.

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- Sould instead require that for all efficient A

$$\Pr[A(1)] = S] \leq 2^{-\alpha n}$$

