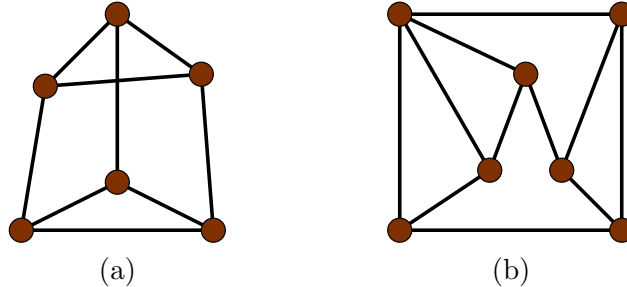


Problem Set 1

Due: Monday, November 8, 2004

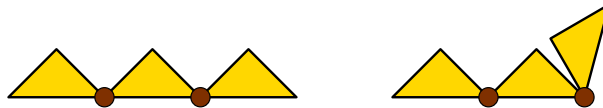
Problem 1. Give a Henneberg construction for each of the following minimally generically rigid graphs.



Problem 2. Prove that every pointed pseudotriangulation is minimally generically rigid. A *pseudotriangulation* of a set of points in the plane is a collection of edges between these points, including the convex hull of the point set, such that every face except the outside face has exactly three convex vertices. A pseudotriangulation is *pointed* if every vertex has an incident reflex angle (angle of more than 180°). Problem 1(b) shows an example of a pointed pseudotriangulation.

Problem 3. Prove that no four-bar 3D open chain is locked.

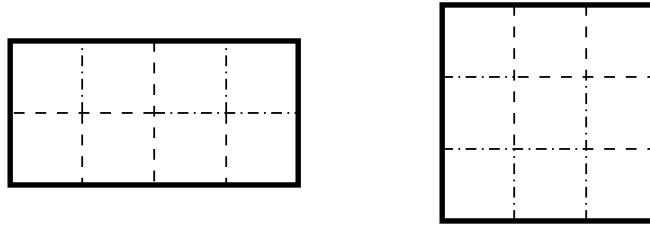
Problem 4. Find a locked planar hinged open chain of convex polygons. An *open chain of polygons* is a collection of polygons P_1, P_2, \dots, P_n where each polygon P_i is joined along one vertex to a vertex of P_{i-1} (if $i > 1$) and joined along a different vertex to a vertex of P_{i+1} (if $i < n$). A *configuration* of such a chain is a rigid placement of the polygons such that joined pairs of vertices are geometrically coincident, and such that no two polygons intersect in their interiors. A *motion* is a continuum of configurations. A chain is *locked* if there are two configurations that cannot reach each other by a motion. Two configurations of the same open chain of polygons are shown below:



Problem 5. Derive and prove a characterization of flat-foldable single-vertex crease patterns where $\theta_1 + \theta_2 + \dots + \theta_n$ might be larger than 360° . You must show that your condition is both necessary and sufficient and that it can be checked in linear time. Give an example of a flat-foldable single-vertex crease pattern that does not satisfy $\theta_1 + \theta_3 + \dots + \theta_{n-1} = \theta_2 + \theta_4 + \dots + \theta_n$.

Problem 6. Find a two-vertex crease pattern that is locally flat foldable (at each vertex) but is not (globally) flat foldable.

Problem 7. Fold the following maps flat using the specified mountain-valley assignment. (Dashed edges are valleys; dot-dashed edges are mountains.)



Problem 8. Fold a pleated hyperbolic paraboloid from a square of paper according to the following directions.

Crease the diagonals	Fold the top edge to the center point, creasing only between the diagonals	Unfold	Repeat on the bottom (fold and unfold)
Fold and unfold on 1/4 and 3/4 marks	Repeat on the bottom	Repeat on left and right sides	Turn over, and crease in between the squares in the opposite direction
Final crease pattern - - - Valley fold - · - · - Mountain fold	Folding the crease pattern completely forms an "X" shape Partially opening it forms a hyper		